Conversion factors

$$ppm_{methane} := 1$$

$$ppm_{NOx} := 1$$

$$ppm_{C1} := 1$$

Ratio between Hydrogen and Carbon atoms in fuel

$$HC_{ratio} := 1.75$$

assumed value although the gasoline is mixed with ethanol

Molecular weights

$$MW_{CO} := 28.01 \frac{gm}{mol} \qquad MW_{CO2} := 44.01 \frac{gm}{mol} \qquad MW_{NO2} := 46.01 \frac{gm}{mol}$$

$$MW_{O2} := 32 \frac{gm}{mol} \qquad MW_{CO} := 12.01 \frac{gm}{mol} \qquad MW_{H} := 1.008 \frac{gm}{mol}$$

$$MW_{CO2} := 44.01 \frac{gm}{mol}$$

$$MW_{NO2} := 46.01 \frac{gm}{mol}$$

$$MW_{O2} := 32 \frac{gm}{mol}$$

$$MW_{C} := 12.01 \frac{gm}{mol}$$

$$MW_{H} := 1.008 \frac{gm}{mol}$$

$$MW_{fuel} := (MW_C + HC_{ratio} \cdot MW_H) = 0.014 \frac{kg}{mol}$$

Total molecular weight of fuel

Calculating NO2 correction factor to account for humidity

$$H_{\text{specific}} := 3.0343 \frac{\text{gm}}{\text{kg}}$$

Specific humidity of air at intake (units are grams of moisture per kg of air)

$$K_{\text{H}} := \frac{1}{1 - 0.0329 \cdot \left(H_{\text{specific}} - 10.71\right)} = 0.74$$

Correction factor for effects of humidity on NO2 formation

Measured engine performance parameters at four operating points

$$N_{\mathbf{m}} := \begin{pmatrix} 4550 \\ 5250 \\ 5950 \\ 7000 \end{pmatrix} \cdot \frac{1}{\min}$$

Measured engine speed

$$T_{\mathbf{m}} := \begin{pmatrix} 20.4 \\ 28 \\ 45.5 \\ 82 \end{pmatrix} \cdot \hat{\mathbf{m}} \cdot \mathbf{lbf}$$

Measured engine torque

$$dm_{\mathbf{f}} := \begin{pmatrix} 0.014 \\ 0.0215 \\ 0.048 \\ 0.136 \end{pmatrix} \cdot \frac{\mathrm{kg}}{15 \cdot \mathrm{s}}$$

Measured mass flow rate of fuel

$$i := 1, 2..4$$

$$P_{m_i} := 2 \cdot \pi \cdot N_{m_i} \cdot T_{m_i} \qquad P_{m} = \begin{pmatrix} 13.179 \\ 20.871 \\ 38.438 \\ 81.497 \end{pmatrix} \cdot kW$$

Calculated power (consistent with recorded value in excel spreadsheet)

Measured dry emmisions at four operating points

$$CO_{dry} := \begin{pmatrix} 0.28 \\ 2 \\ 2.287 \\ 6.97 \end{pmatrix} - \%$$

Carbon monoxide dry emissions

$$CO_{2dry} := \begin{pmatrix} 10.26 \\ 9.72 \\ 10.32 \\ 6.26 \end{pmatrix}.\%$$

Carbon dioxide dry emissions

$$HC_{dry} := \begin{pmatrix} 706 \\ 483 \\ 222 \\ 3450 \end{pmatrix} \cdot ppm_{methane}$$

Hydro-carbon dry emissions

$$NO_{xdry} := \begin{pmatrix} 51\\101\\181\\249 \end{pmatrix} \cdot ppm_{NOx}$$

NOx dry emissions

$$O_{2dry} := \begin{pmatrix} 6.5 \\ 6.02 \\ 2.57 \\ 6.29 \end{pmatrix}.\%$$

Oxygen dry emissions

The correction factor K is the factor used to adjust the dry percentages of each emission which do not include water into the wet percentages which do include water. In order to accomplish this one must calculate the percentage of H2 in the emissions.

$$\begin{split} \mathbf{H}_{2\text{dry}} &:= \frac{0.5 \cdot \text{HC}_{\text{ratio}} \cdot \text{CO}_{\text{dry}} \cdot \left(\text{CO}_{\text{dry}} + \text{CO}_{2\text{dry}} \right)}{\text{CO}_{\text{dry}} + 3 \cdot \text{CO}_{2\text{dry}}} = \begin{pmatrix} 4.153 \\ 4.14 \\ 3.88 \\ 5.01 \end{pmatrix} \cdot \% \\ \mathbf{K}_{\text{ef}} &:= \frac{1}{1 + \left[0.005 \cdot \left(\text{CO}_{\text{dry}} + \text{CO}_{2\text{dry}} \right) \cdot \text{HC}_{\text{ratio}} - 0.01 \cdot \text{H}_{2\text{dry}} \right] \cdot 100} = \begin{pmatrix} 0.952 \\ 0.942 \\ 0.933 \\ 0.938 \end{pmatrix} \end{split}$$

Calculated wet emmisions at four operating points

$$\begin{aligned} &\operatorname{CO}_{wet_i} \coloneqq \mathsf{K}_{cf_i} \cdot \operatorname{CO}_{dry_i} & \operatorname{CO}_{wet} = \begin{pmatrix} 0.266 \\ 1.885 \\ 2.134 \\ 6.541 \end{pmatrix}, \\ &\mathcal{C}_{wet_i} \coloneqq \mathsf{K}_{cf_i} \cdot \operatorname{CO}_{2dry_i} & \operatorname{CO}_{2wet} = \begin{pmatrix} 9.765 \\ 9.16 \\ 9.631 \\ 5.874 \end{pmatrix}, \\ &\mathcal{C}_{wet_i} \coloneqq \mathsf{K}_{cf_i} \cdot \operatorname{CO}_{2dry_i} & \operatorname{CO}_{2wet} = \begin{pmatrix} 671.939 \\ 455.167 \\ 207.185 \\ 3.237 \times 10^3 \end{pmatrix} \\ &\operatorname{Ppm}_{methane} \\ &\operatorname{Hydro-carbon wet emissions} \\ &\operatorname{NO}_{xwet_i} \coloneqq \mathsf{K}_{cf_i} \cdot \operatorname{NO}_{xdry_i} & \operatorname{NO}_{xwet} = \begin{pmatrix} 48.54 \\ 95.18 \\ 168.921 \\ 233.657 \end{pmatrix}, \\ &\operatorname{Ppm}_{NOx} \\ &\operatorname{NOx wet emissions} \\ &\operatorname{O}_{2wet_i} \coloneqq \mathsf{K}_{cf_i} \cdot \operatorname{O}_{2dry_i} & \operatorname{O}_{2wet} = \begin{pmatrix} 6.186 \\ 5.673 \\ 2.398 \\ 5.902 \end{pmatrix}, \\ &\mathcal{O}_{xygen} \end{aligned} \end{aligned}$$

Calculate mass emissions

$$TC_i := \left(CO_{wet_i} + CO_{2wet_i} + \frac{HC_{wet_i}}{10^6}\right)$$
 $TC = \begin{pmatrix} 10.099 \\ 11.09 \\ 11.786 \\ 10.786 \end{pmatrix}$.%

$$TC = \begin{pmatrix} 10.099\\11.09\\11.786\\12.739 \end{pmatrix}.\%$$

$$\mathbf{CO}_{mass_i} \coloneqq \frac{\mathbf{MW_{CO}}}{\mathbf{MW_{fuel}}} \cdot \frac{\mathbf{dm_{f_i}}}{\mathbf{TC_i}} \cdot \mathbf{CO_{wet_i}}$$

$$CO_{\text{mass}} = \begin{pmatrix} 180.306 \\ 1.783 \times 10^{3} \\ 4.242 \times 10^{3} \\ 3.408 \times 10^{4} \end{pmatrix} \cdot \frac{\text{gm}}{\text{hr}}$$

$$\mathbf{CO_{2mass}}_i \coloneqq \frac{\mathbf{MW_{CO2}}}{\mathbf{MW_{fuel}}} \cdot \frac{\mathbf{dm_f}_i}{\mathbf{TC_i}} \cdot \mathbf{CO_{2wet_i}}$$

$$CO_{2\text{mass}} = \begin{pmatrix} 1.038 \times 10^4 \\ 1.362 \times 10^4 \\ 3.008 \times 10^4 \\ 4.809 \times 10^4 \end{pmatrix} \cdot \frac{\text{gm}}{\text{hr}}$$

$$\mathrm{HC}_{mass_i} \coloneqq \frac{\mathrm{dm}_{f_i}}{\mathrm{TC}_i} \cdot \frac{\mathrm{HC}_{wet_i}}{10^6}$$

$$HC_{mass} = \begin{pmatrix} 22.357 \\ 21.178 \\ 20.25 \\ 829.525 \end{pmatrix} \cdot \frac{gm}{hr}$$

$$NO_{xmass_i} := \frac{MW_{NO2}}{MW_{fuel}} \cdot \frac{dm_{f_i}}{TC_i} \cdot \frac{NO_{xwet_i}}{10^6} \cdot K_H$$

$$NO_{xmass} = \begin{pmatrix} 3.989\\ 10.939\\ 40.784\\ 147.891 \end{pmatrix}, \frac{gm}{hr}$$

$$\mathrm{O}_{2mass_i} \coloneqq \frac{\mathsf{MW}_{O2}}{\mathsf{MW}_{fuel}} \cdot \frac{\mathsf{dm}_{f_i}}{\mathsf{TC}_i} \cdot \mathrm{O}_{2wet_i}$$

$$O_{2\text{mass}} = \begin{pmatrix} 4.782 \\ 6.132 \\ 5.446 \\ 35.136 \end{pmatrix} \cdot \frac{\text{kg}}{\text{hr}}$$

Calculate the brake specific emission values

$$\begin{split} bs_{CO_i} &\coloneqq \frac{cO_{mass_i}}{P_{m_i}} & bs_{CO} = \begin{pmatrix} 0.014 \\ 0.085 \\ 0.11 \\ 0.418 \end{pmatrix} \cdot \frac{kg}{hr \cdot kW} & Brake specific carbon monoxide emission \\ bs_{CO2} &\coloneqq \frac{cO_{2mass_i}}{P_{m_i}} & bs_{CO2} = \begin{pmatrix} 0.788 \\ 0.652 \\ 0.783 \\ 0.59 \end{pmatrix} \cdot \frac{kg}{hr \cdot kW} & Brake specific carbon dioxide emission \\ bs_{HC} &\coloneqq \frac{HC_{mass_i}}{P_{m_i}} & bs_{HC} &= \begin{pmatrix} 1.696 \times 10^{-3} \\ 1.015 \times 10^{-3} \\ 5.268 \times 10^{-4} \\ 0.01 \end{pmatrix} \cdot \frac{kg}{hr \cdot kW} & Brake specific hydrocarbon emission \\ bs_{NOx} &\coloneqq \frac{NO_{xmass_i}}{P_{m_i}} & bs_{NOx} &= \begin{pmatrix} 3.027 \times 10^{-4} \\ 1.061 \times 10^{-3} \\ 1.815 \times 10^{-3} \end{pmatrix} \cdot \frac{kg}{hr \cdot kW} & Brake specific NOx emission \\ bs_{O2} &\coloneqq \frac{O_{2mass_i}}{P_{m_i}} & bs_{O2} &= \begin{pmatrix} 0.363 \\ 0.294 \\ 0.142 \\ 0.431 \end{pmatrix} \cdot \frac{kg}{hr \cdot kW} & Brake specific oxygen emission \\ Brake speci$$

Discussion/Reflection: In this problem it was interesting to see how many different pieces of equipment went into monitoring an engine. However, if I think about it there is a lot of phenomena that is going on in such a device. It is nice to see how we can use multi-diciplinary engineering (mechanical, electrical, computer) to optimize performance and still make progress in what is a relatively old technology.